

# Analysis Techniques: Flow Duration Analysis Tutorial

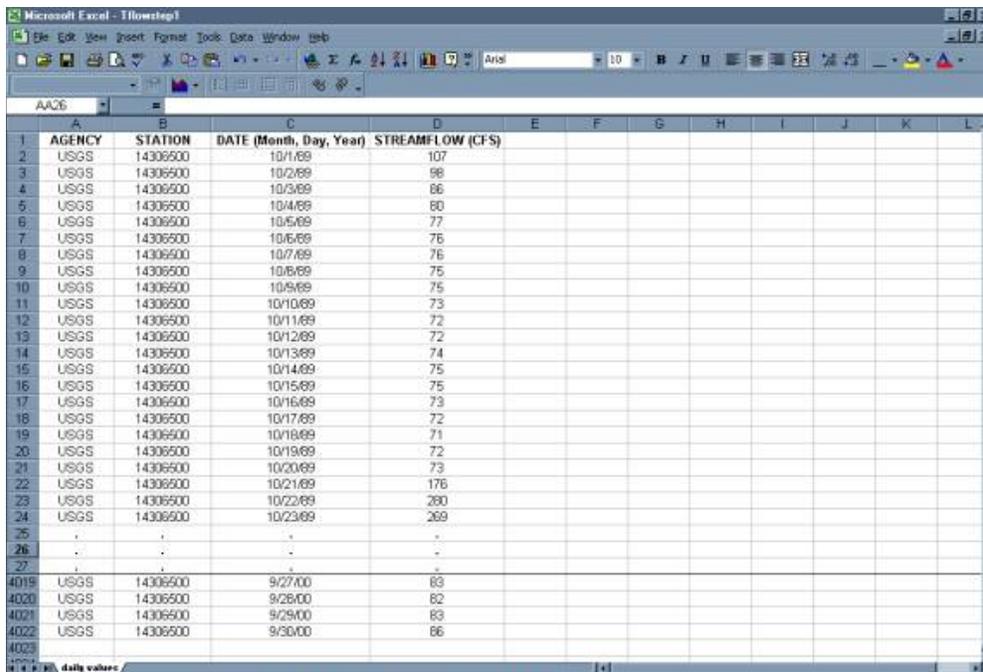
## Information to get started:

- The lesson below contains step-by-step instructions and "snapshots" of what each step looks like when carried out in a Microsoft Excel workbook. Blue shading of information in the Excel illustrations denotes changes made from the previous step. Dots placed in three consecutive rows indicate that a portion of data is hidden from sight.
- You can download an Excel workbook containing the complete data set by clicking on the "Download Data" link below. It contains each calculation step on a separate worksheet. To move between steps, click on the tabs at the bottom of the excel window.
- When you download the file, it may open in your browser window. You may wish to use the "save as" function to save the file to a local drive and then reopen it in Excel. This will make it easier to flip between the online lesson and the example workbook.
- Finally, we want to remind you that the techniques explained on this site are statistically based; therefore results must be viewed as predictions and not as facts. Please use the techniques and the information obtained from them responsibly!

## Download Data

### Step 1: Select the time step value (day, month, etc.) and download the chronological record of discharge

- For the Alsea Example and Tutorial, the analysis will be done using a daily time step.



	A	B	C	D	E	F	G	H	I	J	K	L
1	AGENCY	STATION	DATE (Month, Day, Year)	STREAMFLOW (CFS)								
2	USGS	14306500	10/1/99	107								
3	USGS	14306500	10/2/99	98								
4	USGS	14306500	10/3/99	86								
5	USGS	14306500	10/4/99	80								
6	USGS	14306500	10/5/99	77								
7	USGS	14306500	10/6/99	76								
8	USGS	14306500	10/7/99	76								
9	USGS	14306500	10/8/99	75								
10	USGS	14306500	10/9/99	75								
11	USGS	14306500	10/10/99	73								
12	USGS	14306500	10/11/99	72								
13	USGS	14306500	10/12/99	72								
14	USGS	14306500	10/13/99	74								
15	USGS	14306500	10/14/99	75								
16	USGS	14306500	10/15/99	75								
17	USGS	14306500	10/16/99	73								
18	USGS	14306500	10/17/99	72								
19	USGS	14306500	10/18/99	71								
20	USGS	14306500	10/19/99	72								
21	USGS	14306500	10/20/99	73								
22	USGS	14306500	10/21/99	176								
23	USGS	14306500	10/22/99	280								
24	USGS	14306500	10/23/99	269								
25	.	.	.	.								
26	.	.	.	.								
27	.	.	.	.								
4019	USGS	14306500	9/27/00	83								
4020	USGS	14306500	9/28/00	82								
4021	USGS	14306500	9/29/00	83								
4022	USGS	14306500	9/30/00	86								
4023												

**Step 2: Compute the total number of time step intervals in the period of record.**

The screenshot shows an Excel spreadsheet with the following data:

	A	B	C	D	E	F	G	H	I	J	K	L
	AGENCY	STATION	DATE (Month, Day, Year)	STREAMFLOW (CFS)								
1	USGS	14306500	10/1/69	107								
2	USGS	14306500	10/2/69	98								
3	USGS	14306500	10/3/69	86								
4	USGS	14306500	10/4/69	80								
5	USGS	14306500	10/5/69	77								
6	USGS	14306500	10/6/69	76								
7	USGS	14306500	10/7/69	76								
8	USGS	14306500	10/8/69	75								
9	USGS	14306500	10/9/69	75								
10	USGS	14306500	10/10/69	73								
11	USGS	14306500	10/11/69	72								
12	USGS	14306500	10/12/69	72								
13	USGS	14306500	10/13/69	74								
14	USGS	14306500	10/14/69	75								
15	USGS	14306500	10/15/69	75								
16	USGS	14306500	10/16/69	73								
17	USGS	14306500	10/17/69	72								
18	USGS	14306500	10/18/69	71								
19	USGS	14306500	10/19/69	72								
20	USGS	14306500	10/20/69	73								
21	USGS	14306500	10/21/69	176								
22	USGS	14306500	10/22/69	280								
23	USGS	14306500	10/23/69	269								
24												
25												
26												
27												
4020	USGS	14306500	9/26/00	82								
4021	USGS	14306500	9/29/00	83								
4022	USGS	14306500	9/30/00	86								
4023	<b>DAYS FOR PERIOD OF RECORD</b>			<b>4018</b>								
4024												

### Step 3: Rank discharge by magnitude.

- Use the "sort" command to rank the entries by discharge, from largest to smallest.
- Create a new column called "Rank". Use the excel "rank" function to determine the rank of each discharge in the period of record.

	A	B	C	D	E	F	G	H	I	J	K	L
1	AGENCY	STATION	DATE (Month, Day, Year)	STREAMFLOW (CFS)	Rank							
2	USGS	14306500	2/7/1996	29400	1							
3	USGS	14306500	12/28/1998	28200	2							
4	USGS	14306500	2/8/1996	22300	3							
5	USGS	14306500	11/19/1996	20900	4							
6	USGS	14306500	2/6/1996	20300	5							
7	USGS	14306500	2/9/1996	19800	6							
8	USGS	14306500	11/26/1999	17400	7							
9	USGS	14306500	1/1/1997	16600	8							
10	USGS	14306500	12/29/1998	16300	9							
11	USGS	14306500	12/26/1996	16100	10							
12	USGS	14306500	1/14/1995	15500	11							
13	USGS	14306500	12/31/1996	15300	12							
14	USGS	14306500	12/2/1998	15300	12							
15	USGS	14306500	11/26/1998	15200	14							
16	USGS	14306500	12/30/1996	15100	15							
17	USGS	14306500	2/28/1999	14900	16							
18	USGS	14306500	1/2/1997	14700	17							
19	USGS	14306500	2/24/1999	14700	17							
20	USGS	14306500	12/13/1995	14400	19							
21	USGS	14306500	1/7/1990	13900	20							
22	USGS	14306500	1/15/1995	13900	20							
23	USGS	14306500	12/29/1996	13800	22							
24	USGS	14306500	12/27/1996	13600	23							
25	USGS	14306500	2/7/1999	13400	24							
26	USGS	14306500	11/30/1995	13200	25							
27	USGS	14306500	1/18/1999	13100	26							
28	USGS	14306500	12/12/1995	13000	27							
29	USGS	14306500	1/8/1990	12500	28							
30	USGS	14306500	12/14/1995	12500	28							
31	USGS	14306500	12/1/1995	12400	30							
32	USGS	14306500	1/13/1995	12100	31							
33	USGS	14306500	2/25/1999	12100	31							
34	USGS	14306500	11/25/1998	11900	33							
35	USGS	14306500	12/15/1995	11800	34							

## Step 4: Calculate the percent of time that each discharge is equaled or exceeded.

- Create a new column called "Exceedence Probability". As noted on the [flow duration page](#), the exceedence probability can be calculated as follows:

$$P = 100 * [ M / (n + 1) ]$$

P = the probability that a given flow will be equaled or exceeded (% of time)

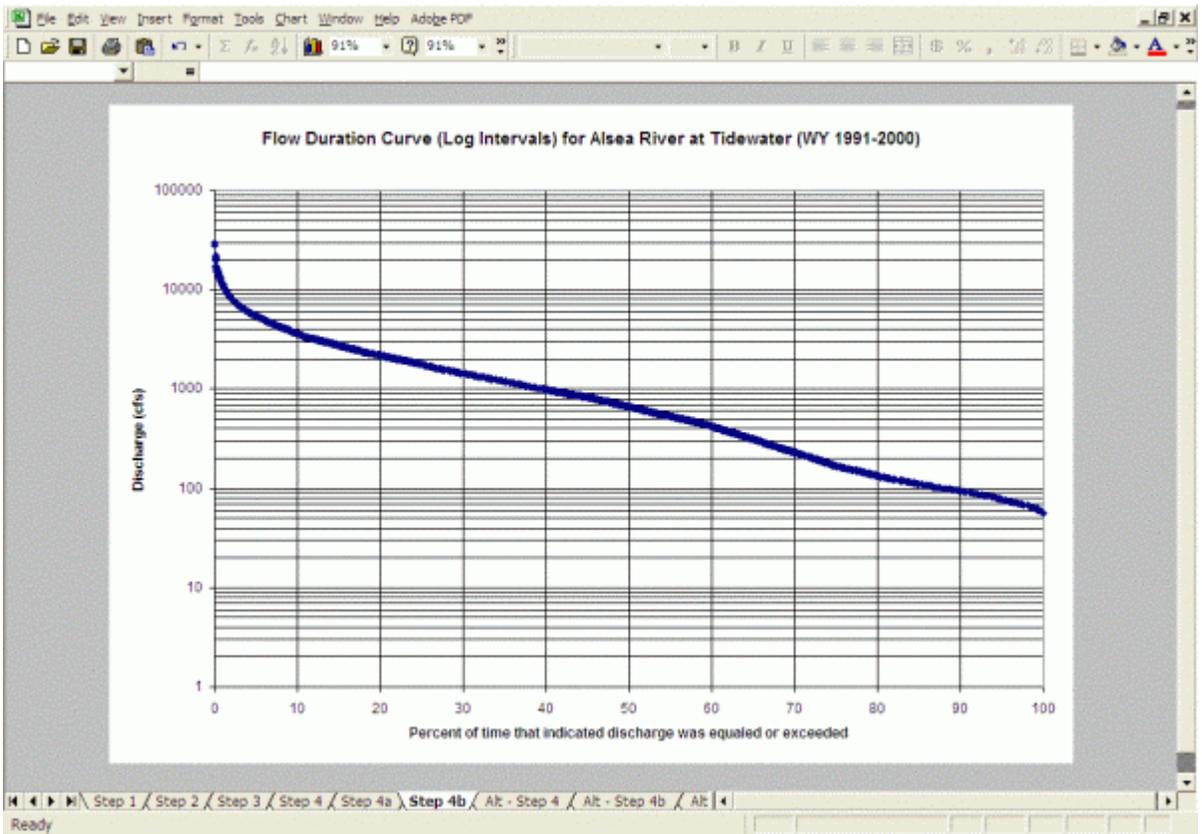
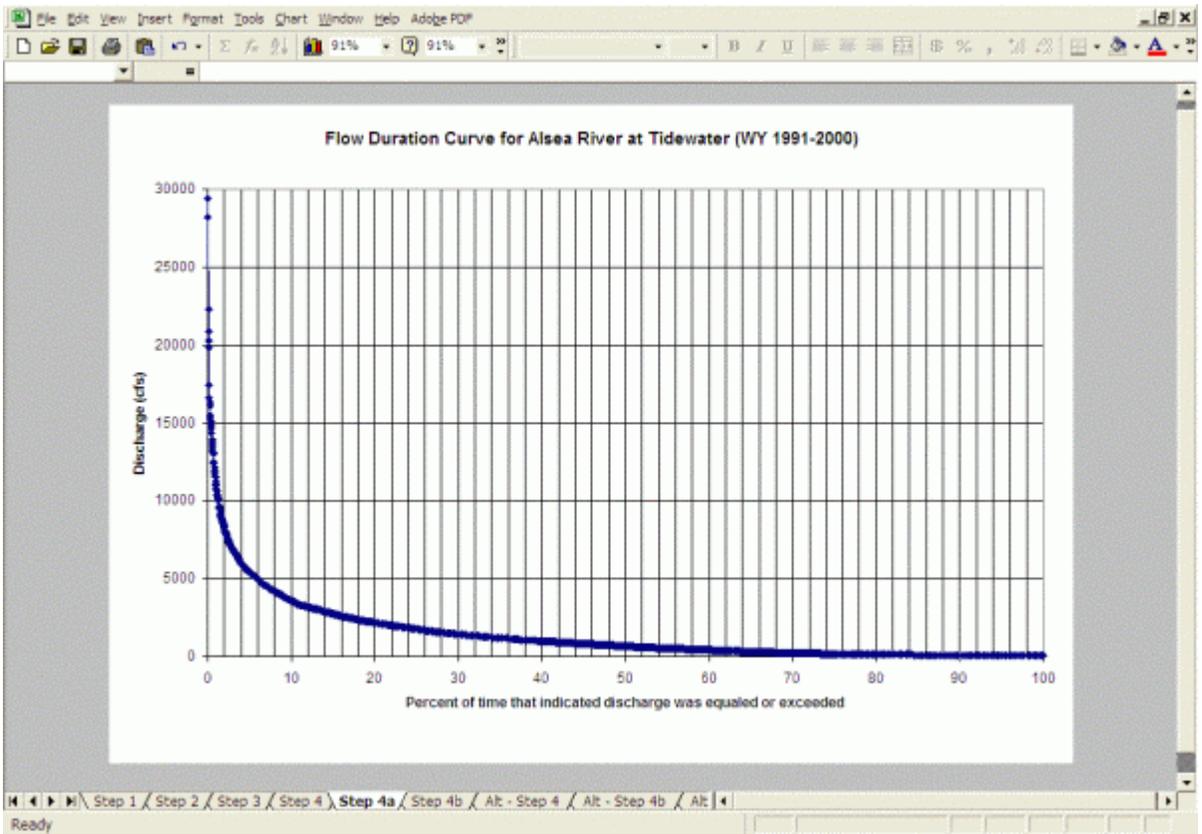
M = the ranked position on the listing (dimensionless)

n = the number of events for period of record (dimensionless)

Create a formula to calculate this value for each record using the information from Step 2  
 (= (E2 / ('Step 2'!\$D\$4020 + 1)) \* 100).

1	A	B	C	D	E	F	G	H	I	J	K
	AGENCY	STATION	DATE (Month, Day, Year)	STREAMFLOW (CFS)	Rank	Percent Exceeded					
2	USGS	14306500	2/7/1996	29400	1	0.025					
3	USGS	14306500	12/28/1998	28200	2	0.050					
4	USGS	14306500	2/8/1996	22300	3	0.075					
5	USGS	14306500	11/19/1996	20900	4	0.100					
6	USGS	14306500	2/6/1996	20300	5	0.124					
7	USGS	14306500	2/9/1996	19800	6	0.149					
8	USGS	14306500	11/26/1999	17400	7	0.174					
9	USGS	14306500	1/1/1997	16600	8	0.199					
10	USGS	14306500	12/29/1998	16300	9	0.224					
11	USGS	14306500	12/26/1996	16100	10	0.249					
12	USGS	14306500	1/14/1995	15500	11	0.274					
13	USGS	14306500	12/31/1996	15300	12	0.299					
14	USGS	14306500	12/2/1998	15300	12	0.299					
15	USGS	14306500	11/26/1998	15200	14	0.348					
16	USGS	14306500	12/30/1996	15100	15	0.373					
17	USGS	14306500	2/28/1999	14900	16	0.398					
18	USGS	14306500	1/2/1997	14700	17	0.423					
19	USGS	14306500	2/24/1999	14700	17	0.423					
20	USGS	14306500	12/13/1995	14400	19	0.473					
21	USGS	14306500	1/7/1990	13900	20	0.498					
22	USGS	14306500	1/15/1995	13900	20	0.498					
23	USGS	14306500	12/29/1996	13800	22	0.547					
24	USGS	14306500	12/27/1996	13600	23	0.572					
25	USGS	14306500	2/7/1999	13400	24	0.597					
26	USGS	14306500	11/30/1995	13200	25	0.622					
27	USGS	14306500	1/18/1999	13100	26	0.647					
28	USGS	14306500	12/12/1995	13000	27	0.672					
29	USGS	14306500	1/8/1990	12500	28	0.697					
30	USGS	14306500	12/14/1995	12500	28	0.697					
31	USGS	14306500	12/1/1995	12400	30	0.746					
32	USGS	14306500	1/13/1995	12100	31	0.771					
33	USGS	14306500	2/25/1999	12100	31	0.771					
34	USGS	14306500	11/25/1998	11900	33	0.821					
35	USGS	14306500	12/15/1995	11800	34	0.846					

- Graph the "exceedence probability" versus the discharge. The graph can have either linear or logarithmic axes.

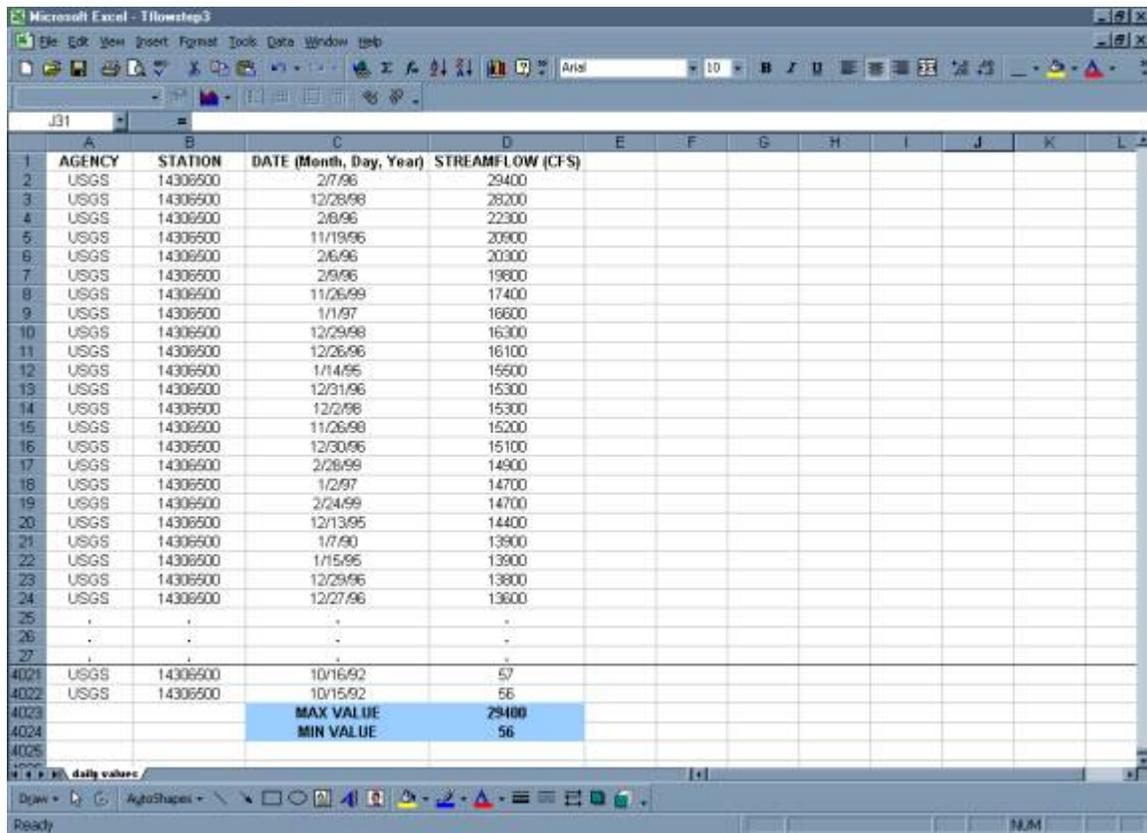


## Alternative Approach:

Before spreadsheet programs were common, flow duration curves were constructed by grouping the data into discharge size classes (bins). This avoided the once time-consuming tasks of sorting, ranking, and graphing the individual discharge records. With modern spreadsheet programs, these steps can be done quickly and flow duration curves can be created as we described above.

However, some flow duration analyses are still made by grouping data into size classes. The steps below will guide you through this alternative approach.

### Alternative Step 3: Rank discharge by magnitude and calculate maximum and minimum discharge.



	A	B	C	D	E	F	G	H	I	J	K	L
	AGENCY	STATION	DATE (Month, Day, Year)	STREAMFLOW (CFS)								
1	USGS	14306500	2/7/96	29400								
3	USGS	14306500	12/26/98	26200								
4	USGS	14306500	2/8/96	22300								
5	USGS	14306500	11/19/96	20900								
6	USGS	14306500	2/6/96	20300								
7	USGS	14306500	2/9/96	19800								
8	USGS	14306500	11/26/99	17400								
9	USGS	14306500	1/1/97	16600								
10	USGS	14306500	12/29/98	16300								
11	USGS	14306500	12/26/96	16100								
12	USGS	14306500	1/14/96	15500								
13	USGS	14306500	12/31/96	15300								
14	USGS	14306500	12/2/98	15300								
15	USGS	14306500	11/26/98	15200								
16	USGS	14306500	12/30/96	15100								
17	USGS	14306500	2/26/99	14900								
18	USGS	14306500	1/2/97	14700								
19	USGS	14306500	2/24/99	14700								
20	USGS	14306500	12/13/95	14400								
21	USGS	14306500	1/7/90	13900								
22	USGS	14306500	1/15/95	13900								
23	USGS	14306500	12/29/96	13800								
24	USGS	14306500	12/27/96	13600								
25	.	.	.	.								
26	.	.	.	.								
27	.	.	.	.								
4021	USGS	14306500	10/16/92	57								
4022	USGS	14306500	10/15/92	56								
4023			MAX VALUE	29400								
4024			MIN VALUE	56								
4025												

## Alternative Step 4: Divide the range of average values into classes.

- Calculate the average value of the variable of interest within each time step (average daily value) for the period of record and note the largest and smallest of these average values.

	A	B	C	D	E	F	G	H	I	J	K	L
1	AGENCY	STATION	DATE (Month, Day, Year)	STREAMFLOW (CFS)								
2	USGS	14306500	2/7/96	29400								
3	USGS	14306500	12/28/98	28200								
4	USGS	14306500	2/8/96	22300								
5	USGS	14306500	11/19/96	20900								
6	USGS	14306500	2/6/96	20300								
7	USGS	14306500	2/9/96	19800								
8	USGS	14306500	11/26/99	17400								
9	USGS	14306500	1/1/97	16800								
10	USGS	14306500	12/29/98	16300								
11	USGS	14306500	12/26/96	16100								
12	USGS	14306500	1/14/96	15500								
13	USGS	14306500	12/31/96	15300								
14	USGS	14306500	12/2/98	15300								
15	USGS	14306500	11/26/98	15200								
16	USGS	14306500	12/30/96	15100								
17	USGS	14306500	2/26/99	14900								
18	USGS	14306500	1/2/97	14700								
19	USGS	14306500	2/24/99	14700								
20	USGS	14306500	12/13/95	14400								
21	USGS	14306500	1/7/90	13900								
22	USGS	14306500	1/15/95	13900								
23	USGS	14306500	12/29/96	13800								
24	USGS	14306500	12/27/96	13600								
25	.	.	.	.								
26	.	.	.	.								
27	.	.	.	.								
4021	USGS	14306500	10/16/92	57								
4022	USGS	14306500	10/15/92	56								
4023			MAX VALUE	29400								
4024			MIN VALUE	56								
4025												

- It is recommended to have between twenty to thirty class intervals for the period of record. Classes can either be equal interval or based on log cycles. Log cycles are often used to sort data because the probability of choosing appropriate interval spacing is higher than if the data were separated into 20 to 30 equal classes. If improper intervals are chosen, the amount of information the flow duration curve can provide is diminished.
  - For the equal interval method, determine the discharge range for each class by dividing the max discharge value by the desired number of size classes. In the tutorial data, the max discharge value is 29400 cfs. That value divided by 20 is 1470. So for twenty size classes with equal intervals in each class, the smallest size class will be discharges between 0-1470 cfs. The second size class will be 1471-2940 cfs and so on, up to the max value.
  - For classes based on log cycles, select classes of discharge values based on a spacing of 1, 1.5, 2, 3, 4, 5, 7, 10, or on multiples of 10 of these values. For the tutorial data, the size classes will be 10-14 cfs, 15-19 cfs, 20-29 cfs on up to 20,000-29,999 cfs.
- Use the ranked data to count the total number of occurrences of values in each class.

20 Equal Class Intervals:

DATE (Month, Day, Year)	STREAMFLOW (CFS)	CLASS # (1-20)
2/7/96	29400	20
12/28/98	28200	20
		2
2/6/96	22300	16
		1
11/19/96	20900	15
		1
2/6/96	20300	14
2/9/96	19800	14
		2
11/26/99	17400	12
1/1/97	16600	12
12/29/98	16300	12
		3
12/26/96	16100	11
1/14/95	15500	11
12/31/96	15300	11
10/14/92	57	1
10/16/92	57	1
10/15/92	56	1
		2842

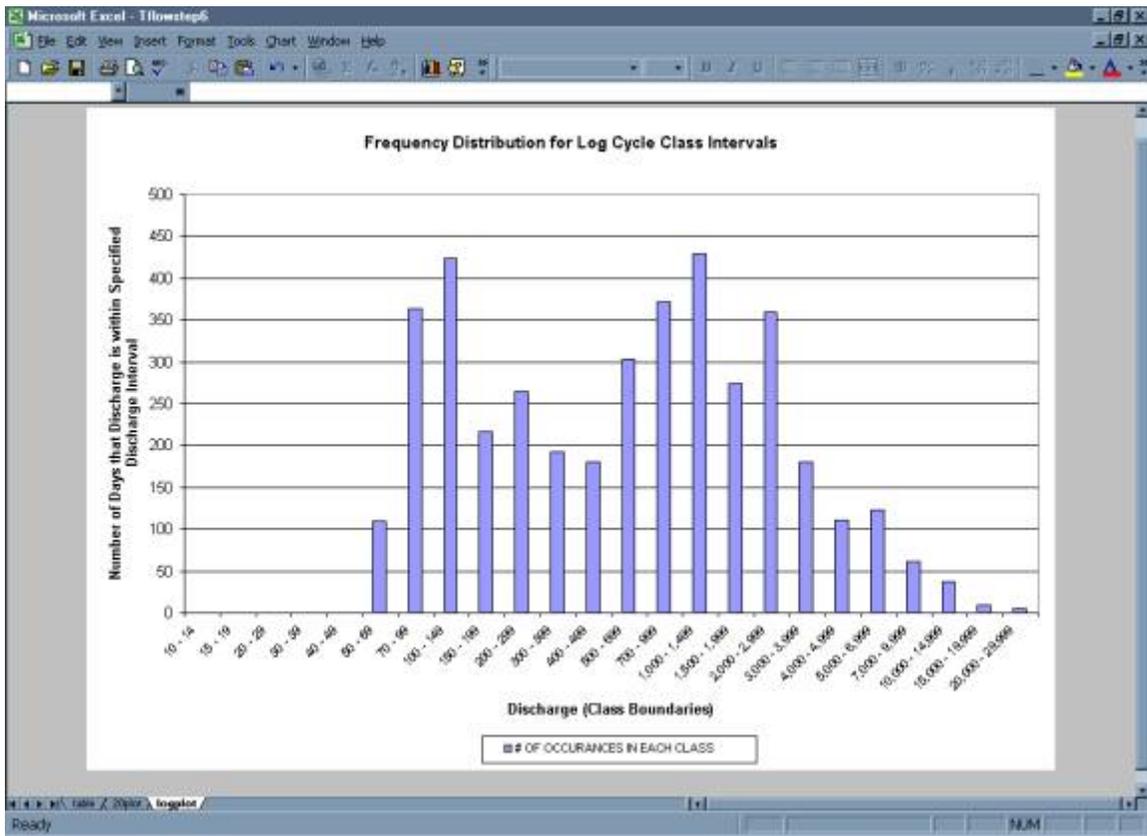
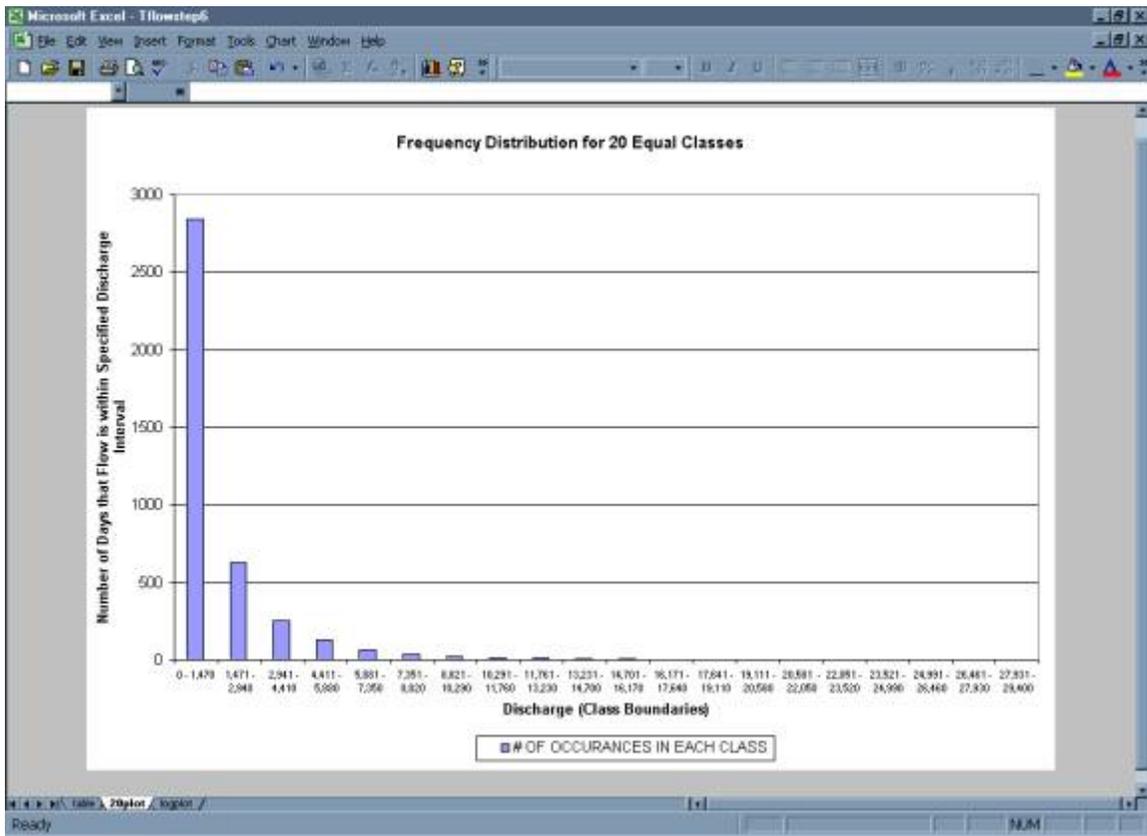
Using Log Cycles:

DATE (Month, Day, Year)	STREAMFLOW (CFS)	CLASS # (1-20)
2/7/96	29400	
12/28/98	28200	
2/6/96	22300	
11/19/96	20900	
2/6/96	20300	
		5
2/9/96	19800	
11/26/99	17400	
1/1/97	16600	
12/29/98	16300	
12/26/96	16100	
1/14/95	15500	
12/31/96	15300	
12/2/99	15300	
11/26/98	15200	
12/30/96	15100	
		10
2/28/99	14900	
1/2/97	14700	
2/24/99	14700	
10/14/92	57	
10/16/92	57	
10/15/92	56	
		109

**Alternative Step 5: Summarize the results in a table.**

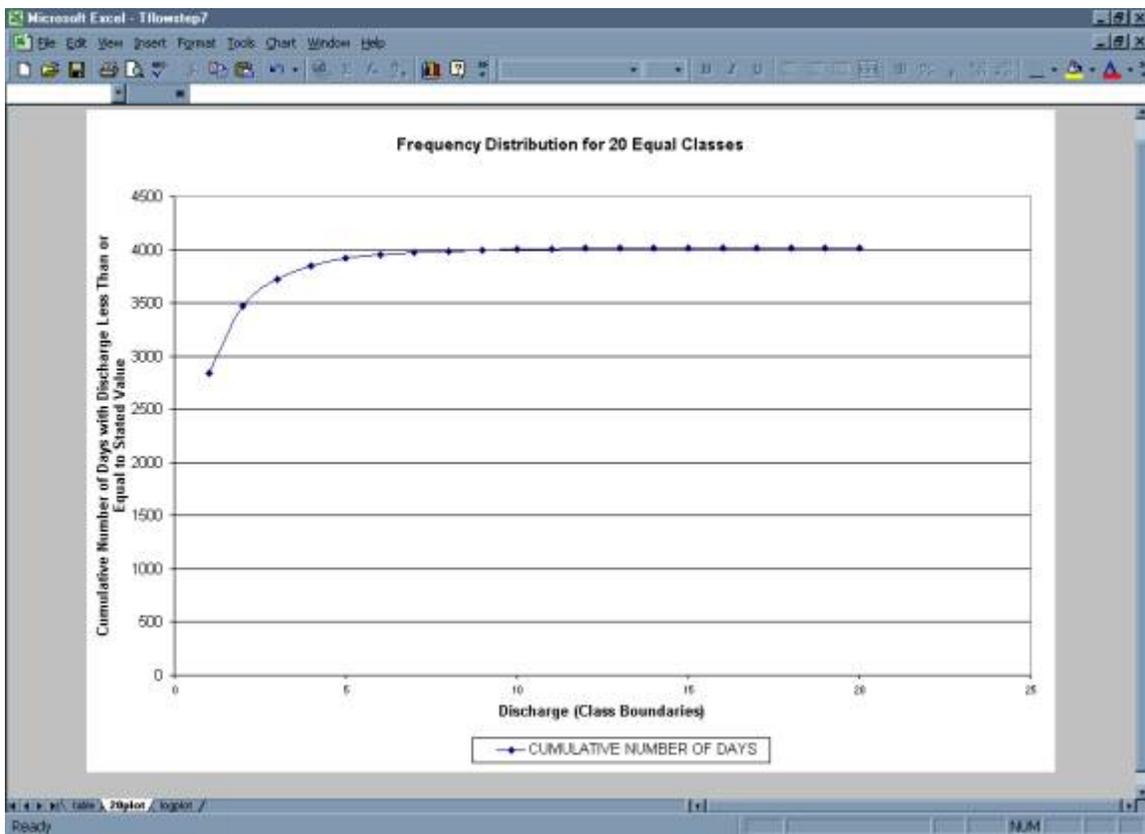
20 EQUAL CLASSES			LOG CYCLE INTERVALS		
	CLASS BOUNDARIES	# OF OCCURANCES IN EACH CLASS		CLASS BOUNDARIES	# OF OCCURANCES IN EACH CLASS
1	0 - 1,470	2842		10 - 14	0
2	1,471 - 2,940	626		15 - 19	0
3	2,941 - 4,410	256		20 - 29	0
4	4,411 - 5,880	128		30 - 39	0
5	5,881 - 7,350	65		40 - 49	0
6	7,351 - 8,820	33		50 - 69	109
7	8,821 - 10,290	21		70 - 99	363
8	10,291 - 11,760	12		100 - 149	424
9	11,761 - 13,230	11		150 - 199	217
10	13,231 - 14,700	8		200 - 299	266
11	14,701 - 16,170	7		300 - 399	192
12	16,171 - 17,640	3		400 - 499	180
13	17,641 - 19,110	0		500 - 699	304
14	19,111 - 20,580	2		700 - 999	372
15	20,581 - 22,050	1		1,000 - 1,499	429
16	22,051 - 23,520	1		1,500 - 1,999	274
17	23,521 - 24,990	0		2,000 - 2,999	360
18	24,991 - 26,460	0		3,000 - 3,999	180
19	26,461 - 27,930	0		4,000 - 4,999	111
20	27,931 - 29,400	2		5,000 - 6,999	123
				7,000 - 9,999	62
				10,000 - 14,999	38
				15,000 - 19,999	10
				20,000 - 29,999	5

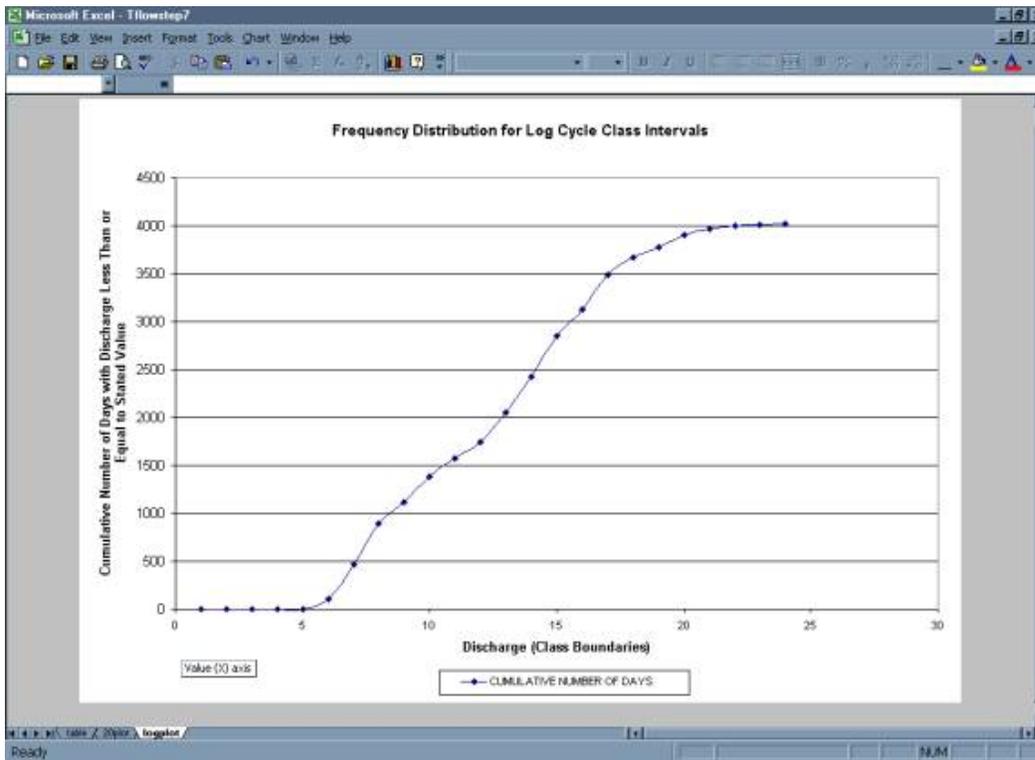
- A plot of the total number of occurrences in each class versus discharge gives a frequency distribution.



**Alternative Step 6: Beginning with the upper boundary of the highest class, add up the total number of values that are greater than the lower boundary for each successive class.**

20 EQUAL CLASSES				LOG CYCLE INTERVALS			
	CLASS BOUNDARIES	NUMBER OF DAYS IN EACH CLASS	CUMULATIVE NUMBER OF DAYS	CLASS BOUNDARIES	NUMBER OF DAYS IN EACH CLASS	CUMULATIVE NUMBER OF DAYS	
1							
2							
3							
4	1	0 - 1,470	2842	10 - 14	0	0	
5	2	1,471 - 2,940	626	15 - 19	0	0	
6	3	2,941 - 4,410	256	20 - 29	0	0	
7	4	4,411 - 5,880	128	30 - 39	0	0	
8	5	5,881 - 7,350	65	40 - 49	0	0	
9	6	7,351 - 8,820	33	50 - 69	109	109	
10	7	8,821 - 10,290	21	70 - 99	363	472	
11	8	10,291 - 11,760	12	100 - 149	424	896	
12	9	11,761 - 13,230	11	150 - 199	217	1113	
13	10	13,231 - 14,700	8	200 - 299	265	1378	
14	11	14,701 - 16,170	7	300 - 399	192	1570	
15	12	16,171 - 17,640	3	400 - 499	180	1750	
16	13	17,641 - 19,110	0	500 - 699	304	2054	
17	14	19,111 - 20,580	2	700 - 999	372	2426	
18	15	20,581 - 22,050	1	1,000 - 1,499	429	2855	
19	16	22,051 - 23,520	1	1,500 - 1,999	274	3129	
20	17	23,521 - 24,990	0	2,000 - 2,999	360	3489	
21	18	24,991 - 26,460	0	3,000 - 3,999	180	3669	
22	19	26,461 - 27,930	0	4,000 - 4,999	111	3780	
23	20	27,931 - 29,400	2	5,000 - 6,999	123	3903	
24				7,000 - 9,999	62	3965	
25				10,000 - 14,999	39	4003	
26				15,000 - 19,999	10	4013	
27				20,000 - 29,999	5	4018	
28							





### Alternative Step 7: The cumulative number of occurrences is converted to a percentage of the time.

- Divide the values developed above by the total number of time steps from Step 2; this gives the frequency with which the lower values of each class have been equaled or exceeded in the period of record.

20 EQUAL CLASSES							
	CLASS BOUNDARIES	NUMBER OF DAYS IN EACH CLASS	CUMULATIVE NUMBER OF DAYS	PERCENT OF TIME FLOW IS NOT EXCEEDED (%)	PERCENT OF TIME FLOW IS EQUALED OR EXCEEDED (%) (100-% NOT EXCEEDED)	CLASS BOUNDARIES	
1							
2							
3							
4	1	0 - 1,470	2842	70.73	29.27	10	
5	2	1,471 - 2,940	626	86.31	13.69	15	
6	3	2,941 - 4,410	256	92.68	7.32	20	
7	4	4,411 - 5,880	128	95.87	4.13	30	
8	5	5,881 - 7,350	65	97.49	2.51	40	
9	6	7,351 - 8,820	33	98.31	1.69	50	
10	7	8,821 - 10,290	21	98.83	1.17	70	
11	8	10,291 - 11,760	12	99.13	0.87	100	
12	9	11,761 - 13,230	11	99.40	0.60	150	
13	10	13,231 - 14,700	8	99.60	0.40	200	
14	11	14,701 - 16,170	7	99.78	0.22	300	
15	12	16,171 - 17,640	3	99.85	0.15	400	
16	13	17,641 - 19,110	0	99.85	0.15	500	
17	14	19,111 - 20,580	2	99.90	0.10	700	
18	15	20,581 - 22,050	1	99.93	0.07	1,000	
19	16	22,051 - 23,520	1	99.95	0.05	1,500	
20	17	23,521 - 24,990	0	99.95	0.05	2,000	
21	18	24,991 - 26,460	0	99.95	0.05	3,000	
22	19	26,461 - 27,930	0	99.95	0.05	4,000	
23	20	27,931 - 29,400	2	100.00	0.00	5,000	
24						7,000	
25						10,000	

Microsoft Excel - Flow Duration DL Tutorial

LOG CYCLE INTERVALS

CLASS BOUNDARIES	NUMBER OF DAYS IN EACH CLASS	CUMULATIVE NUMBER OF DAYS	PERCENT OF TIME FLOW IS NOT EXCEEDED (%)	PERCENT OF TIME FLOW IS EQUALED OR EXCEEDED (%) (100% NOT EXCEEDED)
10 - 14	0	0	0.00	100.00
15 - 19	0	0	0.00	100.00
20 - 29	0	0	0.00	100.00
30 - 39	0	0	0.00	100.00
40 - 49	0	0	0.00	100.00
50 - 69	109	109	2.71	97.29
70 - 99	363	472	11.75	88.25
100 - 149	424	896	22.30	77.70
150 - 199	217	1113	27.70	72.30
200 - 299	265	1378	34.30	65.70
300 - 399	192	1570	39.07	60.93
400 - 499	180	1750	43.55	56.45
500 - 699	304	2054	51.12	48.88
700 - 999	372	2426	60.38	39.62
1,000 - 1,499	429	2855	71.06	28.94
1,500 - 1,999	274	3129	77.07	22.93
2,000 - 2,999	360	3489	86.83	13.17
3,000 - 3,999	180	3669	91.31	8.69
4,000 - 4,999	111	3780	94.08	5.92
5,000 - 6,999	123	3903	97.14	2.86
7,000 - 9,999	62	3965	98.68	1.32
10,000 - 14,999	39	4003	99.63	0.37
15,000 - 19,999	10	4013	99.88	0.12
20,000 - 29,999	5	4018	100.00	0.00

**Alternative Step 8: Finally the diagram is turned so that discharge is given on the vertical axis and exceedence frequency is given on the horizontal axis.**

